Example Assignment

Foundations of Computational Math

Due date: 11:59PM on September 23rd 2048

Problem

Consider the forward, backward, and central difference approximations to the derivative of f at x, respectively:

1. $F_h[f](x) = \frac{f(x+h) - f(x)}{h}$ 2. $B_h[f](x) = \frac{f(x) - f(x-h)}{h}$ f(x+h) - f(x-h)

3.
$$C_h[f](x) = \frac{f(x+h) - f(x-h)}{2h}$$

Analyze the absolute error in the above numerical approximations as $h \to 0$, for the following:

1.
$$f_1(x) = \sin(x)$$
 at $x = 1.0$ and $x = 2.0$.

2.
$$f_2(x) = \exp\left(-\frac{x^2}{2}\right)$$
 at $x = 1.1$ and $x = 2.2$.

Confirm numerically the order (with respect to h) of the respective numerical approximations.