

1. Determine if the statement is True or False and give a (short) supporting reason.

(a) $\{z : 1 < |z| \leq 2\}$ is open.

(b) $\{z : |z - i| = 1\}$ is a circle of radius 1 centered at $-i$.

(c) If $w_1, w_2 \in \mathbb{C}$ and z_1 is a root of the polynomial $p(z) = z^2 + w_1z + w_2$, then \bar{z}_1 is also a root of $p(z)$.

(d) $(1 + i)^{10} = 32i$

(e) $\{z : |z + i| \geq |z - i|\} = \{z : \Im z \geq 0\}$

(f) $\text{Arg}(z_1 z_2) = \text{Arg } z_1 + \text{Arg } z_2 + n2\pi$ for n either -1, 0 or 1.

(g) $1/z = \bar{z}/|z|^2$

(h) $z^2 - \bar{z}^2 = 1$ is the equation of a hyperbola

(i) $i^{55} = -i$

(j) $\lim_{z \rightarrow -\infty} 1/z = 0$