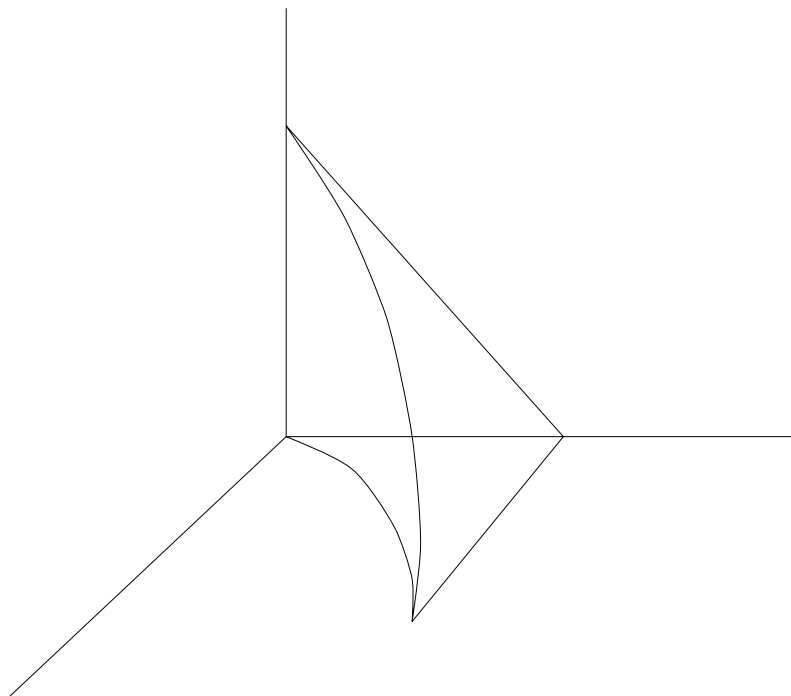


Show **ALL** work for credit; be neat; and use only **ONE** side of each page of paper.

- Find the curl and div of $\mathbf{F} = \langle x^2y, yz^2, zx^2 \rangle$.
- Find f so that $\mathbf{F} = \nabla f$ and use it to find the line integral $\int_C \mathbf{F} \cdot d\mathbf{r}$. Here $\mathbf{F} = \langle 2xz + \sin y, x \cos y, x^2 \rangle$ and C is a curve from $(1, 0, 0)$ to $(1, 0, 2\pi)$.
- Evaluate the line integral $\int_C x^2y dx - 3y^2 dy$ using Green's Theorem when C is the curve which goes around the perimeter of the region $\{(x, y) : 0 \leq x \leq 1, 0 \leq y \leq 1\}$ in the backwards (clockwise) direction.
- Find the equation of the tangent plane to the parametric surface given by $\langle u^2, u - v^2, v^2 \rangle$ at the point $(1, 0, 1)$.
- Rewrite but do **NOT** evaluate the surface integral $\int \int_S \mathbf{F} \cdot d\mathbf{S}$ as an usual double iterated integral (including limits of integration and a simplified integrand). Here $\mathbf{F} = \langle y, x, xy \rangle$ and S is the portion of the paraboloid $z = x^2 + 2y^2$ over the region $\{(x, y) : 1 \leq x \leq 2, \ln x \leq y \leq \pi\}$ Use the upward pointing normal of S .
- Set up but do **NOT** evaluate a double iterated integral for the surface area of the surface $z = y^2 - x^2$ that lies between the cylinders $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$. The double iterated integral needs to have limits of integration and a simplified integrand.
- Use cylindrical co-ordinates to evaluate $\int \int \int_E x^2 dV$ when E is the solid within $x^2 + y^2 = 1$, above $z = 0$ and below $z^2 = 4x^2 + 4y^2$.
- Evaluate the line integral $\int_C \mathbf{F} \cdot d\mathbf{r}$ if $\mathbf{F} = \langle x^2y, -xy \rangle$, and $\mathbf{r}(t) = \langle t^3, t^4 \rangle, 0 \leq t \leq 1$.
- Use the given transformation to evaluate $\int \int_R x dA$ where R is the region in the **FIRST** quadrant where $9x^2 + 4y^2 \leq 36$ and the transformation is $x = 2u, y = 3v$. Also explicitly draw R and S , the region in the uv plane that maps to R in the xy plane by this transformation. Clearly label the Jacobian of the transformation.
- Rewrite the the limits of $\int_0^1 \int_{\sqrt{x}}^1 \int_0^{1-y} f(x, y, z) dz dy dx$ in the orders $dx dy dz$ and $dy dz dx$.



Hint