

1. Determine if the statement is True or False and give a (short) supporting reason.
 - (a) The singularities of $\csc z$ are all simple poles.
 - (b) $\sin z/z$ has a removable singularity at $z = 0$ and is thus really an entire function.
 - (c) If $z = 0$ is a pole of order 5 for $f(z)$, then $f(1/z)$ is a polynomial of degree 5.
 - (d) For $a > 0$, $\int_{-\infty}^{\infty} (a^2 + \theta^2)^{-1} d\theta = \pi/a$
 - (e) If $g(z)$ is entire, then the residue of $f(z)g(z)$ at $z = z_0$ is the residue of $f(z)$ at $z = z_0$ times $g(z_0)$.
 - (f) $(\sum a_n z^n)(\sum b_n z^n) = \sum a_n b_n z^{2n}$
 - (g) In the region where both sides are defined, $1/(1 + z + z^2 + z^3 + \dots) = 1 - z$
 - (h) If $f(z)$ is bounded near its singularity at $z = z_0$ then $z = z_0$ is a pole for $f(z)$.
 - (i) The residue of $\text{Log } z$ at $z = 0$ is 1.
 - (j) The residue of $\exp(iz)/z$ at $z = 0$ is $1/2$