

Closing in on the Mechanisms of Pulsatile Insulin Secretion

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Insulin secretion from pancreatic islet β -cells occurs in a pulsatile fashion, with a typical period of ~5 min. The basis of this pulsatility in mouse islets has been investigated for more than four decades, and the various theories have been described as either qualitative or mathematical models. In many cases the models differ in their mechanisms for rhythmogenesis, as well as other less important details. In this Perspective, we describe two main classes of models: those in which oscillations in the intracellular Ca²⁺ concentration drive oscillations in metabolism, and those in which intrinsic metabolic oscillations drive oscillations in Ca2+ concentration and electrical activity. We then discuss nine canonical experimental findings that provide key insights into the mechanism of islet oscillations and list the models that can account for each finding. Finally, we describe a new model that integrates features from multiple earlier models and is thus called the Integrated Oscillator Model. In this model, intracellular Ca²⁺ acts on the glycolytic pathway in the generation of oscillations, and it is thus a hybrid of the two main classes of models. It alone among models proposed to date can explain all nine key experimental findings, and it serves as a good starting point for future studies of pulsatile insulin secretion from human islets.

Insulin secretion in healthy rodents, dogs, and humans is pulsatile, with mean period of \sim 5 min (1). This pulsatility has been reported to enhance insulin action at the liver (2), although not all studies have shown this (3). The consequences of pulsatile insulin secretion and its dysfunction in people with or at risk for type 2 diabetes has been recently reviewed (4). The focus of this Perspective, rather, is the mechanism of insulin pulsatility, in particular the rhythmogenesis of \sim 5-min oscillations in activity of pancreatic

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Pulsatility in insulin secretion reflects oscillations in the intracellular Ca^{2+} concentration of islet β -cells, which in turn reflect bursting electrical activity (5). In intact islets, several types of oscillations are commonly observed. Slow oscillations have periods typically between 4 and 6 min (Fig. 1A). Fast oscillations are observed in other islets, with periods typically less than 1 min (Fig. 1B). Fast oscillations can also be packaged into episodes to form "compound oscillations," and the episodes repeat with the same range of periods as the pure slow oscillations (Fig. 1C). The compound Ca²⁺ oscillations reflect a type of electrical activity called "compound bursting" (6,7). Both slow and compound Ca2+ oscillations have periods consistent with measurements of plasma insulin in mice (8). In human islet β-cells, most electrical oscillations reported thus far are of the fast type, but slow oscillations in the Ca²⁺ concentration have been observed (Fig. 2) and have similar periodicity to pulsatile insulin secretion (4). Human islets tend to have larger action potentials than rodent islets owing to the prominent Na⁺ currents, but the similarity of the slow oscillation periods suggests that the underlying mechanisms are similar in rodents and humans.

In the search for the biophysical mechanisms of oscillations in β -cell activity, several classes of models (both qualitative and mathematical) have emerged. We describe the key elements of these models, along with experimental findings that should be explainable by any proposed model. We conclude with a description of one recent model, the Integrated Oscillator Model (IOM), which combines features

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Figure 1—Intracellular electrical recordings from islet β -cells exhibiting three types of oscillations. *A*: Example of islet with slow oscillations. *B*: An islet exhibiting fast oscillations. *C*: An islet with compound oscillations composed of episodes of fast oscillations. Recordings were made using perforated patch and amphotericin B. Ren and Satin, unpublished data.

of prior models and satisfies all the experimental tests described herein.

We focus on the interactions of Ca^{2+} and metabolism in generating slow oscillations, omitting discussion of other interesting areas that have been the subject of mathematical modeling (as in Fridlyand et al. [9]), such as cAMP oscillations, synchronization within and among islets, and exocytosis. Some have suggested that other factors, such as cAMP, islet paracrine factors, and insulin itself may play roles in β -cell oscillations, but because of space restrictions we do not discuss these hypotheses.

HYPOTHESES FOR ISLET OSCILLATIONS

In 1983 Chay and Keizer (10) published a pioneering β -cell model that spawned many subsequent models. At its core was slow negative feedback, a ubiquitous mechanism for oscillations, whereby a rise in intracellular free Ca²⁺ activates Ca²⁺-activated K⁺ channels (K_{Ca} channels). According to this model, the rise of intracellular Ca²⁺ during a burst active phase and its decline during a silent phase drives bursting through its action on K_{Ca} channels. This model was successful at reproducing the fast (i.e., 15-s period) burst pattern predominantly reported in the literature at the time, as well as the response of the cell to changes in glucose. That is, at low glucose levels the cell is silent, at higher levels it bursts, and at the highest levels it produces

a continuous train of impulses. Within the bursting regimen, increases in the glucose level increase the active phase duration relative to the silent phase duration, known as the "plateau fraction."

Shortly after the publication of this model, ATP-sensitive K^+ channels (K_{ATP} channels) were first reported in β -cells (11). The importance of these channels in setting insulin secretion to a level appropriate for the prevailing blood glucose concentration was immediately recognized, but their existence also raised the possibility that oscillations in metabolism could underlie oscillations in the cells' electrical activity, Ca²⁺ level, and insulin secretion. Indeed, there have been numerous subsequent measurements of metabolic oscillations in islets, including oscillations in oxygen consumption, NAD(P)H, and mitochondrial membrane potential, as reviewed in Bertram et al. (12).

The two main classes of models for β -cell oscillations can be categorized into those in which oscillations in Ca²⁺ drive oscillations in metabolism (Ca²⁺-driven oscillations) and those in which oscillations in metabolism drive oscillations in Ca²⁺ (metabolism-driven oscillations). The many models constituting the first class differ in the specific biophysical components most important for electrical activity and Ca²⁺ oscillations. In all cases, however, bursting electrical activity (Fig. 3A) reflects slow negative feedback through one or more slow processes that we represent by a single slow



Figure 2—Oscillations in intracellular Ca²⁺ concentration in five different human islets loaded with the ratiometric dye Fura-PE3 AM. All show slow oscillations, similar to what is often observed in mouse islets.

variable *s*. During the active phase, *s* slowly rises and ultimately terminates spiking, while during the silent phase it slowly declines, eventually becoming small enough for electrical activity to begin again. This variable therefore has a sawtooth time course (Fig. 3*B*). In some models, metabolic oscillations occur as a result of Ca^{2+} -dependent ATP production (13,14) or Ca^{2+} -dependent ATP consumption by Ca^{2+} pumps (15–17). In other variants, the slow negative feedback that drives bursting is not provided directly by Ca^{2+} but by voltage-dependent inactivation of Ca^{2+} channels (13,18) or by the accumulation of Na⁺, possibly mediated by the Na⁺/Ca²⁺ exchanger, which in turn activates Na⁺/K⁺ pumps (16,17) or a combination of ionic mechanisms (17,19). In all these cases, however, the metabolic oscillations are due to oscillations in Ca^{2+} .

The alternative idea that metabolic oscillations drive Ca^{2+} oscillations in β -cells was first proposed by Tornheim (20), based on the observation that oscillations in glycolysis can be measured in muscle extracts (21) and are due to the muscle isoform (PFK-M) of the key glycolytic enzyme phosphofructokinase (PFK). In this step, fructose 6-phosphate (F6P) is converted to fructose 1,6-bisphosphate (FBP), which is an allosteric activator of PFK-M activity. This same isoform is present in β -cells and is the most active



Figure 3—Computer simulations of a model in which bursting electrical activity is driven by activity-dependent variation in a slow process *s*. *A*: Electrical bursting, characterized by periodic active phases of spiking and silent phases of membrane hyperpolarization. *B*: Sawtooth time course of *s*.

PFK isoform (22). The hypothesis is that glycolytic oscillations occur in glucose-stimulated β -cells and that these lead to oscillations in ATP production, which modulates K_{ATP} channels, driving electrical bursting and Ca^{2+} oscillations. This is the template for the second general class of models.

The Dual Oscillator Model (DOM) combines elements of the two major classes and postulates that Ca²⁺ oscillations drive the fast electrical bursting in β -cells, while glycolytic oscillations, when active, drive slow bursting (12). Compound bursting is driven by both processes, the fast bursts within an episode being driven by Ca^{2+} feedback onto K_{Ca} channels, whereas the pacing of the episodes is controlled by glycolytic oscillations and ATP/ADP action on KATP channels. The model was recently modified to add negative feedback of Ca²⁺ onto the metabolic pathway (23). This change improved agreement between our newer experimental observations while preserving the previous advantages of the DOM. The joint participation of Ca²⁺ feedback and glycolysis in slow oscillations, which makes the model neither purely Ca²⁺-driven nor metabolism-driven, motivates the name "Integrated Oscillator Model."

KEY EXPERIMENTAL FINDINGS

Table 1 lists experimental findings that provide particularly useful constraints for biophysical models of oscillatory islet activity. The first three rows of Table 1 indicate which models can account for fast, slow, and compound oscillations. (Two models [15,20] are qualitative rather than mathematical models, so we have to infer the behaviors they could produce.) Compound oscillations are the most challenging to explain and are most robustly accounted for by models which have metabolism-driven oscillations as well as Ca²⁺ feedback onto K⁺ channels (the DOM and IOM).

	Models with Ca ²⁺ -driven oscillations	Models with metabolism-driven oscillations
Fast bursting and Ca ²⁺ patterns	CK83, KM89, SK92, D98, F03, BS04, C11, Dd06	DOM, IOM
Slow bursting and Ca ²⁺ patterns	D98, BS04, C11, Dd06	T97, DOM, IOM
Compound bursting and Ca ²⁺ patterns	B08	DOM, IOM
Subthreshold oscillations	None	T97, DOM, IOM
Metabolic oscillations with Ca ²⁺ clamped by Dz	None	DOM, IOM
Oscillations in K _{ATP} conductance measured with voltage ramps during islet bursting	None	T97, DOM, IOM
Ca ²⁺ oscillations stimulated by KIC	CK83, KM89, SK92, D98, F03, BS04, C11, Dd06	IOM
Sawtooth oscillations in Perceval	CK83, KM89, SK92, D98, F03, BS04, C11, Dd06	IOM
Sawtooth oscillations in PKAR	None	IOM
B08. Bertram et al., 2008 (48): BS04. Bertram and Sherman, 2004 (49): C11. Cha et al., 2011 (17): CK83. Chav and Keizer, 1983 (10): D98.		

Table 1-Key experimental findings and the models that can replicate them

B08, Bertram et al., 2008 (48); BS04, Bertram and Sherman, 2004 (49); C11, Cha et al., 2011 (17); CK83, Chay and Keizer, 1983 (10); D98, Detimary et al., 1998 (15); Dd06, Diederichs, 2006 (50); DOM, Bertram et al., 2007 (27); F03, Fridlyand et al., 2003 (16); IOM, McKenna et al., 2016 (23); KM89, Keizer and Magnus, 1989 (40); SK92, Smolen and Keizer, 1992 (13); T97, Tornheim, 1997 (20).

The next experimental finding (row 4, Table 1) is oscillations in K_{ATP} conductance (24) or Ca²⁺ concentration (25) seen in the presence of subthreshold glucose concentrations. In this case, the K_{ATP} conductance is too large to allow action potentials, but small oscillations in the membrane potential can sometimes be observed (Thompson and Satin, unpublished data). The data cited suggest that metabolic oscillations in metabolism, and concomitant small amplitude oscillations in Ca²⁺, do not require electrical bursting oscillations.

A direct way to discriminate between Ca^{2+} -driven metabolic oscillations and metabolism-driven Ca^{2+} oscillations is to clamp one of the two variables and determine whether the other still oscillates. Clamping cytosolic Ca^{2+} has been done using diazoxide (Dz), which opens K_{ATP} channels and thereby hyperpolarizes β -cells (row 5, Table 1). It was found that the metabolic oscillations present in stimulatory glucose were terminated by the application of Dz (26,27), which suggested that metabolic oscillations require Ca^{2+} oscillations. It was later shown that metabolic oscillations can in fact persist under these conditions in some islets (i.e., in Dz and without Ca^{2+} oscillations) and that even in islets where Dz initially abrogates the metabolic oscillations they can often be rescued by elevating Ca^{2+} by adding KCl to Dz to depolarize the islet while Ca^{2+} remains steady (Fig. 4) (28).

Another way to clamp the Ca^{2+} level of a β -cell in an islet is to use patch clamping to fix the membrane potential (row 6, Table 1). In stimulatory glucose, the rest of the islet will continue to exhibit electrical activity while the patched cell is held at the clamp command potential. In Ren et al. (29), voltage ramps were used to generate current-voltage curves from the patched cell while the rest of the islet displayed slow bursting electrical activity. Analysis of the data revealed slow oscillations in K_{ATP} conductance, with lower conductance during the active phases of the bursts than during the silent phases (Fig. 5). The K_{ATP} oscillations likely resulted from metabolic oscillations in the clamped cells, as the Ca²⁺ level was nonoscillatory because of the voltage clamp. As seen in Fig. 5*B*, the K_{ATP} conductance has a square shape rather than the sawtooth shape in Fig. 3*B*, indicating that the metabolic oscillations occurred in pulses under these conditions.

An alternative to clamping Ca^{2+} is to clamp metabolism and determine whether electrical bursting and Ca^{2+} oscillations persist. This has been attempted using the fuel α -ketoisocaproic acid (KIC), which enters metabolism at the citric acid cycle, bypassing glycolysis (row 7, Table 1). Some studies have shown that KIC can induce Ca^{2+}



Figure 4—Measurement of PKAR, which reflects dynamics in the FBP concentration. The islet is initially exposed to 10 mmol/L glucose (G), then 0.2 mmol/L Dz is added, and finally KCI (K) is added. Oscillations that are eliminated by the Dz are rescued by depolarization when the KCI concentration is increased from 15 to 30 mmol/L. Reprinted with permission from Merrins et al. (35).



Figure 5—Measurement of the K_{ATP} channel conductance made from a patched cell in an islet exposed to 11.1 mmol/L glucose. *A*: Slow bursting produced when the patch electrode is in current clamp mode. *B*: K_{ATP} channel conductance when the patch electrode is in voltage clamp mode with the application of rapid voltage ramps (2-s ramps from -120 mV to -50 mV). Red symbols identify the conductance during the active phases of two bursts; there are clear pulses of reduced conductance during the bursts. Panels *A* and *B* are sequential, not aligned. Protocol similar to that used in Ren et al. (29). nS, nanosiemens.

oscillations with period of several minutes, even in the absence of glucose; these oscillations are qualitatively similar to those induced by glucose alone (30,31). This observation is not universal, however, as Ca²⁺ oscillations were not observed in two studies that used the same KIC concentration (32,33). In the cases where KIC-induced Ca^{2+} oscillations were observed, they could not have resulted from glycolytic oscillations. Although these data pose no challenge to the class of models with Ca²⁺-induced metabolic oscillations, they are a substantial challenge to models in which Ca²⁺ oscillations are driven by metabolic oscillations. Recently, however, it was demonstrated that the IOM can account for KIC-induced Ca²⁺ oscillations (23) caused by the utilization of ATP by Ca^{2+} pumps, which is the mechanism described by Detimary et al. (15) and above. This differs from glucose-induced oscillations in the IOM, which are driven primarily by the glycolytic subsystem and Ca²⁺ feedback onto mitochondrial dehydrogenases, as explained below. Note that the predicted shapes of ATP and Ca²⁺ are very similar for these two mechanisms, so it is difficult to know which mechanism is driving the oscillations without simultaneously measuring a glycolytic metabolite.

A real-time fluorescent readout of the ATP time course has been made using the ATP-sensing fluoroprotein Perceval or its improved variant Perceval-HR (34). These studies showed that the ATP/ADP ratio in the cytosol (35) or submembrane space of the β -cells (36) exhibited sawtooth oscillations in response to stimulatory glucose (row 8, Table 1). A slow decline in ATP/ADP was observed throughout the active phase of the burst and a slow rise during the silent phase. This would be expected if oscillations are driven by the mechanism proposed in Detimary et al. (15). During the active phase, Ca^{2+} is elevated, so ATP slowly declines as a result of hydrolysis by Ca^{2+} ATPase pumps, in turn reactivating the K_{ATP} channels. During the silent phase, Ca^{2+} is low, so ATP slowly rises, inhibiting K_{ATP} channels and ultimately starting a new active phase. The IOM, which includes this mechanism, can also account for the sawtooth shape of ATP/ADP (23).

The final row of Table 1 refers to an experimental study that used a Förster resonance energy transfer biosensor (pyruvate kinase activity reporter, or PKAR [37]) that is sensitive to FBP to monitor the time course of the product of the key glycolytic enzyme PFK-M. PKAR, a direct probe of glycolytic oscillations, was found to oscillate in glucosestimulated islets with a sawtooth pattern (37). Moreover, simultaneous measurements of PKAR and membrane potential (Fig. 6A) or Ca^{2+} revealed that PKAR (and thus FBP) typically declines during the burst active phase and rises during the silent phase (35). Such FBP oscillations would not be predicted by models in which metabolic oscillations are driven by Ca²⁺ feedback downstream of glycolysis. The DOM, which is based on intrinsic slow glycolytic oscillations, also failed to account for the sawtooth pattern of the FBP oscillations or their phase relationship to Ca²⁺ oscillations (35). This deficiency was overcome in the IOM by incorporating Ca^{2+} stimulation of pyruvate dehydrogenase, as we discuss next. Although a sawtooth PKAR pattern was most common, a subset of islets exhibited more pulsatile PKAR oscillations (Fig. 6B), which is also consistent with the IOM (Fig. 7H and McKenna and Bertram [unpublished data]).

THE INTEGRATED OSCILLATOR MODEL

The IOM builds on the DOM by adding a key Ca²⁺ feedback to glycolysis (23). Glucose metabolism involves several



Figure 6—PKAR measurements from two bursting islets with very different time courses. A: Sawtooth PKAR time course, measured simultaneously with the membrane potential from a patched cell. B: Pulsatile PKAR time course.

Ca²⁺-activated dehydrogenases involved in the production of NADH and FADH₂. In particular, pyruvate dehydrogenase (PDH), which converts pyruvate to acetyl-CoA and immediately precedes the citric acid cycle, is strongly activated by Ca²⁺ (38). We describe next how this Ca²⁺ feedback impacts glycolysis to shape the time course of FBP and ATP in the model.

In the DOM, glycolytic oscillations are driven by feedback of the product FBP onto its synthetic enzyme, PFK-M. This positive feedback results in the regenerative production of FBP until its precursor, F6P, becomes substantially depleted. This depletion greatly reduces FBP production until the substrate has built up again. This process of growth, decline, and renewal results in oscillations having a period of \sim 5 min (39). Glucose is the primary input to the system; if it is low, the rate of FBP production will be too low to produce glycolytic oscillations (Fig. 7A). If the glucose level is too high, then F6P will not be depleted, so FBP production will be high and nonoscillatory (Fig. 7C). Only at intermediate values will slow oscillations occur (Fig. 7B), and the FBP time course will be pulsatile. The top row of Fig. 7 schematizes the control of the glycolytic oscillator by glucose influx in the DOM. In Fig. 7A–C the box shown represents glycolysis, including the positive feedback of FBP on PFK-M, and the glucose level (or influx of F6P) is represented by the width of the input channel to glycolysis. The output of glycolysis, pyruvate, is ultimately metabolized in the mitochondria to form ATP, which inhibits PFK-M and hence lowers the rate of glycolysis, as indicated in Fig. 7. ATP

also closes K_{ATP} channels, as indicated, and its concentration is reduced by Ca^{2+} owing to Ca^{2+} pump hydrolysis (15).

In the DOM, we did not consider the effect of the glycolytic efflux rate on the glycolytic oscillations, but it is as important as the effect of the glycolytic influx rate. Thus, if the output of the glycolytic pathway is constricted, as illustrated in Fig. 7D, then the FBP concentration will build up, which would terminate glycolytic oscillations, similar to the case of high glucose influx (Fig. 7C), but termination now occurs because of excessive positive feedback by FBP. At the other extreme, if the efflux rate is very high (Fig. 7F), then the FBP generated by PFK-M would be quickly metabolized, resulting in low FBP and thus insufficient positive feedback onto PFK-M. There would again be no glycolytic oscillations, similar to the case of low glucose influx (Fig. 7A); with high glycolytic efflux, however, ATP production would be large, whereas with low glucose ATP production would be small.

In the IOM, Ca^{2+} regulates glycolytic efflux through its stimulation of PDH, as indicated by the gray shadowing in Fig. 7G. When cytosolic Ca^{2+} is low, glycolytic efflux will be reduced (solid channel in Fig. 7G), causing FBP to accumulate. When Ca^{2+} is high, glycolytic efflux will be high (gray channel in Fig. 7G), causing FBP to decline. When Ca^{2+} oscillates, FBP will have a sawtooth-shaped time course, rising during the down phase of a Ca²⁺ oscillation when FBP efflux is low and declining during the up phase when FBP efflux is high, in agreement with the PKAR data shown in Fig. 6A (row 9 of Table 1). Downstream ATP production will inherit this time course, rising when Ca²⁺ is low and falling when Ca²⁺ is high, in agreement with Perceval and Perceval-HR measurements (row 8 of Table 1). Even though both the Ca^{2+} hydrolysis mechanism (15) and the inhibition of ATP production by mitochondrial Ca²⁺ influx (40) can also account in a natural way for the sawtooth time course of ATP, neither can account for the sawtooth time course of FBP. While there is also evidence for positive feedback of Ca^{2+} on glycolysis at glucokinase (41), this would not yield the observed sawtooth shape of FBP.

Although the IOM generates sawtooth-shaped FBP and ATP oscillations when Ca²⁺ is free to oscillate, pulses of FBP and ATP are predicted when Ca²⁺ is not freely oscillating. For example, at low glucose there should be minimal electrical activity, so Ca^{2+} should be low with perhaps small fluctuations. Although glycolytic oscillations do not typically occur in low glucose in which there is no bursting electrical activity, in some cases they appear to do so, resulting in pulses of FBP and ATP (12,25). Whereas FBP pulses have not yet been observed experimentally in substimulatory glucose, evidence for ATP oscillations have been observed indirectly (row 4 of Table 1) through recordings of K_{ATP} channel activity (24). Ca²⁺ oscillations are also prohibited when a β -cell in an islet is voltage-clamped in stimulatory glucose (as in Ren et al. [29]), but, as described above, we observed the pulse-shaped KATP channel conductance oscillations predicted by the IOM (row 6 of Table 1 and Fig. 5).



Figure 7—Effects of glycolytic input and output on FBP and ATP. *A*–*F*: DOM; *G*–*I*: IOM. In each panel, the box represents the core glycolytic oscillator, in which positive feedback of FBP on PFK supplies the drive. *A*: With low glucose influx, both FBP and ATP levels are low and steady. *B*: With intermediate glucose influx, pulsatile oscillations of FBP result. *C*: With high glucose influx, both FBP and ATP levels are high and steady. *D*: With moderate glucose influx and low glycolytic efflux, the FBP level will be high but the ATP level will be low. *E*: Glycolytic oscillations can occur with moderate glucose influx and moderate glycolytic efflux, resulting in pulses of FBP and ATP, as in panel *B*. *F*: With moderate glucose influx and high glycolytic efflux, FBP is low but ATP level is high. *G*: In the IOM, Ca²⁺ modulates the glycolytic efflux through stimulation of PDH. With low Ca²⁺ glycolytic efflux is now to channel), and with high Ca²⁺ it is high (gray output channel). This results in sawtooth-shaped FBP and ATP time courses. *H*: The IOM can produce pulsatile FBP oscillations in ATP and Ca²⁺ can occur due to the hydrolysis of ATP that powers Ca²⁺ purps. Other models in which Ca²⁺ drives metabolic oscillations can account for this, but not for any of the other panels. Thicker arrows indicate greater flux.

In an informative experiment, Ca^{2+} was clamped in the entire islet by Dz and subsequently elevated by KCl, but we saw NAD(P)H oscillations (28). We also observed NAD(P)H oscillations in SUR1^{-/-} islets lacking Ca²⁺ oscillations (28), providing further evidence that metabolic oscillations can occur without Ca²⁺ oscillations (row 5 of Table 1 and Fig. 4).

In the IOM, the application of Dz to normal islets would lower cytosolic Ca^{2+} concentration, constricting the efflux from glycolysis, which would increase FBP (Fig. 7*D*). However, low Ca^{2+} would also increase ATP as a result of reduced Ca^{2+} pumping, so that PFK-M would be partially inhibited. This would have the opposite effect on the FBP concentration, causing it to decrease. The competition between these opposing actions was clearly shown using PKAR (35); Dz in stimulatory glucose raised PKAR activity initially to a plateau, indicating elevated cytosolic FBP, followed by a decline. When KCl was added later, increasing intracellular Ca^{2+} , the PKAR signal quickly declined, indicating the dominance of the Ca^{2+} induced increase in glycolytic efflux (as in Fig. 7*F*).

The IOM also accounts for our observation of pulsatile PKAR even when Ca^{2+} is unclamped, much like the original DOM. This can happen in the model if glycolytic efflux is in the permissive intermediate regimen when Ca^{2+} is low (Fig. 7*H*). Unlike the DOM, the efflux rate oscillates with Ca^{2+} in

the IOM, but glycolytic oscillations dominate, resulting in pulsatile FBP.

Figure 7*I* illustrates the effect of the fuel KIC, which enters metabolism in the citric acid cycle. When applied in the absence of glucose the glycolytic pathway is bypassed, illustrated by a very low level of FBP. KIC increases ATP production, elevating the ATP level and closing K_{ATP} channels. Ca^{2+} feedback on ATP consumption (15) or production (40) can then produce electrical bursting and Ca^{2+} oscillations (row 7 of Table 1) that are totally independent of glycolysis (23). Other models in which metabolic oscillations are driven by Ca^{2+} oscillations similarly predict ATP oscillations in response to KIC but do not account for metabolic oscillations in the absence of Ca^{2+} oscillations.

SUMMARY AND CONCLUSIONS

There appear to be several mechanisms for slow and compound Ca^{2+} oscillations, which correspond to the observed ~ 5 min period of plasma insulin oscillations. The IOM suggests that the metabolic oscillations seen when Ca^{2+} is clamped are due to intrinsic glycolytic oscillations driven by the allosteric enzyme PFK-M. When Ca^{2+} is not clamped, the IOM suggests that metabolic, Ca^{2+} , and electrical oscillations again involve the glycolytic pathway, but in this case

 Ca^{2+} feedback onto glycolytic output, through activation of pyruvate dehydrogenase, is responsible for the sawtooth pattern observed in FBP, as assessed by the Förster resonance energy transfer sensor PKAR. A third oscillation mechanism appears operative when the fuel KIC is used with little or no glucose, preventing glycolytic oscillations; here the hydrolysis of ATP to power Ca²⁺ pumps is the key controlling element. The IOM suggests (23) that a similar nonglycolytic mechanism may also be responsible for the slow Ca²⁺ oscillations that have been reported in islets from PFK-M knockout mice (42).

Why are there so many mechanisms for slow oscillations? As insulin pulsatility is important for insulin's downstream targets, the system may have evolved to include redundancy to maintain pulsatility. It is noteworthy that when slow Ca^{2+} oscillations have been seen in KIC in the absence of glucose, their periods have been very similar to the oscillations seen in glucose alone (30). This suggests that the various mechanisms are part of an integrated system organized to produce the canonical 5-min period independent of fuel availability; it is difficult to see how independent pathways would produce the same result.

We believe the field is closing in on a comprehensive model of slow oscillations. We acknowledge, however, that while the IOM can account for the key experimental observations, many of its details await experimental verification. Although there is good evidence that a rise in Ca^{2+} is sufficient to reduce ATP (36), we lack quantitative data proving that ATP depletion is sufficient to mediate the role ascribed to it in the model. Tests to perturb mitochondrial Ca²⁺ uptake are needed to ascertain whether the assumed effects occur and are of appropriate magnitude to mediate their claimed functions. Not all studies have found the expected increase in NAD(P)H and FADH₂ by Ca^{2+} (43); the coexistence of positive and negative sites of Ca²⁺ action can lead to diverse responses that are difficult to disentangle. The prediction mentioned earlier of metabolic oscillations during subthreshold Ca²⁺ oscillations awaits confirmation, and the relative prevalence of pulse- and sawtooth-shaped oscillations of FBP remains to be systematically investigated. Metabolic oscillations are synchronized across islets (37), but it is not known whether this is mediated by diffusion of metabolites across gap junctions or secondarily to synchronization of membrane potential and Ca²⁺. The mechanisms underlying observations of slow Ca²⁺ oscillations in islets lacking K_{ATP} channels (44,45) are also not yet established, but a compensation mechanism has been suggested (46); oscillations have been reported to occur in some islets deprived of KATP channels for only 20 min, so compensation may be more rapid than previously appreciated (47). Finally, our focus on the slow oscillations leaves unclear the physiological significance of the fast oscillations.

The progress detailed here in rodents provides a framework to investigate the applicability of the model to human islets. Although there is considerable evidence for disturbed pulsatility in type 2 diabetes in humans, as reviewed by Satin et al. (4), further study of the relative contributions of altered patterning and reduced β -cell mass to secretion is called for. The challenge ahead is to efficiently use our accumulated knowledge of mouse islets to understand the oscillations in the more important (to us) human islets and identify new therapeutic targets that can restore normal pulsatile patterns to patients with type 2 diabetes.

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