

11.2 - Arithmetic Sequences

A sequence of numbers $a_1, a_2, a_3, \dots, a_n, \dots$ is called an **arithmetic sequence** if there is a constant d , called the common difference, such that $a_n = a_{n-1} + d$, for every $n > 1$.

Solving for d : $d = a_n - a_{n-1}$

The ***nth term of an Arithmetic Sequence*** is:

$a_n = a_1 + (n - 1)d$, with a_1 =first term; d =common difference.

The ***sum of the first n terms*** of an Arithmetic Sequence is:

$$S_n = \frac{n}{2}(a_1 + a_n) \quad \text{or, in alternate form,} \quad S_n = \frac{n}{2}(2a_1 + (n - 1)d)$$

11.3 - Geometric Sequences

A sequence of numbers $a_1, a_2, a_3, \dots, a_n, \dots$ is called a **geometric sequence** if there is a constant r , called the common ratio, such that $a_n = ra_{n-1}$, for every $n > 1$, $r \neq 0$.

Solving for r : $r = \frac{a_n}{a_{n-1}}$

The ***nth term of a geometric sequence*** is:

$a_n = a_1 r^{n-1}$, where a_1 =first term; r =common ratio.

The ***Sum of the First N Terms*** of a Geometric Sequence is:

$$S_N = a \frac{1 - r^N}{1 - r}, r \neq 0, 1$$

where a = first term, r = common ratio.

The ***Sum of an Infinite Geometric Series*** $S = \sum_{k=1}^{\infty} ar^{k-1}$ with common

ratio $|r| < 1$ is: $S = \frac{a}{1 - r}$, where a = first term, r = common ratio.