

With $v(t) = mg(1 - e^{-kt/m})/k$ we have

$$\begin{aligned}h(t) &= h_0 - \int_0^t v(\tau) d\tau \\&= h_0 - \frac{mg}{k} \left\{ \int_0^t 1 d\tau - \int_0^t e^{-k\tau/m} d\tau \right\} \\&= h_0 - \frac{mg}{k} \left\{ t - \left(-\frac{m}{k} e^{-k\tau/m} \right) \Big|_0^t \right\} \\&= h_0 - \frac{mg}{k} \left\{ t - \frac{m}{k} (1 - e^{-kt/m}) \right\}\end{aligned}$$

The solution in the back of the book appears to assume that the body is falling upwards.