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Show sufficient work and clearly mark your answers. Each problem is worth 10 points.

1. Bill loans Ted 40000 over a 20 -year period. Ted repays bill with annual payments of 2000 plus interest on the unpaid balance at an annual effective interest rate of $3 \%$. Each payment Bill receives is invested in an account that pays an annual effective interest rate of $5 \%$. Determine the annual effective yield for Bill over the 20-year period.
(A) $3.8 \%$
(B) $3.9 \%$
(C) $4.0 \%$
(D) $4.1 \%$
(E) $4.2 \%$
2. A loan of 100,000 is repaid with monthly deposits of 1000 as long as necessary, plus a final deposit of $X, 0<X<1000$, payable at the same time as the last regular payment of 1000. Interest on the loan is charged using a nominal interest rate of $6 \%$, compounded monthly. Determine $X$.
(A) 950
(B) 960
(C) 970
(D) 980
(E) 990
3. A 20 -year bond with semiannual coupons is bought to yield $4 \%$ annual effective over the first ten years and $6 \%$ annual effective thereafter. The accumulation of discount for the $3^{\text {rd }}$ installment is 5 and the accumulation of discount for the $38^{\text {th }}$ installment is 21.96. Determine the total write-up on the bond from the end of the $5^{\text {th }}$ year to the end of the $15^{\text {th }}$ year.
(A) 198
(B) 209
(C) 217
(D) 226
(E) 234
4. Ed repays a 10 -year loan of 100000 using the sinking fund method, making monthly payments. His total monthly payment, including interest to the lender and deposit into the sinking fund, is 950 . The sinking fund interest rate is $9 \%$ compounded monthly. At the end of 10 years, Ed finds that he must make an additional payment of 3242.86 to repay the loan. Determine the nominal rate of interest compounded monthly that the lender is charging Ed for the loan.
(A) $2.4 \%$
(B) $5.4 \%$
(C) $6.0 \%$
(D) $8.4 \%$
(E) 17.4\%
5. Sue purchases a 1000 par value 20 -year bond with $8 \%$ semiannual coupons and redemption value of 1200 at a price to yield $6 \%$ compounded semiannually. Sue invests each coupon received in an account that pays $10 \%$ compounded semiannually. Immediately after receiving the $12^{\text {th }}$ coupon, Sue sells the bond to a buyer at a price that yields the buyer $8 \%$ compounded semiannually. Determine Sue's nominal yield, compounded semiannually, over the time in which he owns the bond.
(A) $4.65 \%$
(B) $4.70 \%$
(C) $4.75 \%$
(D) $4.80 \%$
(E) $4.85 \%$
6. A special 30-year bond with annual coupons has an initial coupon of 50 and each subsequent coupon is $2 \%$ greater than its previous coupon. The redemption value is 1000. Determine the amortization of premium for year 14 if the bond is bought to yield $2 \%$ annual effective.
(A) 27.03
(B) 28.84
(C) 30.70
(D) 32.68
(E) 34.82
7. A 20-year loan is repaid with annual payments, the first payment being made one year after loan inception. Interest on the loan is $8 \%$ annual effective. The first payment equals 1000 and each subsequent payment is 100 more than its preceding payment. Determine the outstanding balance on the loan immediately after the $5^{\text {th }}$ payment.
(A) 16,225
(B) 16,400
(C) 16,750
(D) 17,275
(E) 17,625
8. A 1000 face value 40 -year callable bond with $5 \%$ annual coupons may be called at the end of any year beginning with the $20^{\text {th }}$ year. If the bond is called before the $30^{\text {th }}$ year, then the redemption value is 1400 . If the bond is called during or after the $30^{\text {th }}$ year, then the redemption value is 1200 . If the bond is not called then it matures at a redemption value of 1100 . The bond is bought at the maximum price that guarantees an annual yield of at least $3 \%$. Determine the annual yield on the bond if the bond was never called.
(A) $3.00 \%$
(B) $3.02 \%$
(C) $3.04 \%$
(D) $3.06 \%$
(E) $3.08 \%$
9. A 5 -year loan is repaid using the amortization method with equal monthly payments. The amount of interest paid in the $54^{\text {th }}$ payment equals two-thirds of the amount of interest paid in the $47^{\text {th }}$ payment. Determine the proportion of the $40^{\text {th }}$ payment that repays principal.
(A) $1 / 4$
(B) $1 / 5$
(C) $1 / 6$
(D) $1 / 7$
(E) $1 / 8$
10. Carol purchases an annual level coupon bond at a price to yield $5 \%$ annual effective. During the $12^{\text {th }}$ year, the amount of interest earned is 64.50 and the principal adjustment is -25.80 . Determine the price Carol paid for the bond.
(A) 1075
(B) 1200
(C) 1325
(D) 1450
(E) 1575
