MAC 2313 Calculus 3

Mini-Test 1

21Jan2004

Directions: Show **ALL** work for credit; Give **EXACT** answers when possible; Start each problem on a **SEPARATE** page; Use only **ONE** side of each page; Be neat; Leave margins on the left and top for the **STAPLE**; Calculators can be used for graphing and calculating only; Nothing written on this page will be graded;

- 1. Let P(-2, 2, 0), Q(1, 3, -1) and R(-4, 2, 1). Find the equation of the plane S throught the points P, Q and R and the area of the triangle $\triangle PQR$.
- 2. Find the center and radius of the sphere S given by the equation $x^2 + y^2 + z^2 4x + 6y 2z = 2$. The graph of S intersects the *xz*-plane in a circle, what is its equation, its center and its radius.
- 3. A particle moving with speed S hits a barrier at an angle of $\pi/3$ and bounces off at at an angle of $\pi/3$ in the opposite direction with the speed reduced by 20 percent. (See the figure below). Find the velocity vectors of the object both before and after impact.



- 4. Using vector operations write $\vec{a} = \langle -3, 2, 5 \rangle$ as the sum of two vectors $\vec{w} + \vec{v}$, where \vec{w} is parallel to \vec{b} and \vec{v} is perpendicular to \vec{b} , when $\vec{b} = \langle -1, 0, 2 \rangle$.
- 5. Find parametric equations of the line of intersection of the two planes x-y-z = 1 and 11x+5y-5z = 20.