1. Is it possible for a Cauchy sequence to have a divergent subsequence? Either give an example, or prove this is impossible.

2. Give an example of two series \( \sum a_n \) and \( \sum b_n \) that both diverge, but so that \( \sum a_n b_n \) converges.