

HOW TO RESOLVE SINGULARITIES?

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Given a polynomial of $n > 2$ variables $x = (x_1, \dots, x_n)$, say $f(x)$ with real or complex coefficients, I will talk about how to find birational transforms $x = \phi(y)$ such that $f(\phi(y))$ are *simplified*, i.e. monomials in local coordinates everywhere.

In the language of algebraic geometry, given an algebraic variety X in an ambient smooth manifold Z , the task is to find a proper birational map $\pi : Z' \rightarrow Z$ such that $\pi^{-1}(X)$ has only normal crossings.

My talk will be about the method to construct π as a finite succession of elementary transformations which are called blowing-ups.

In this talk, I will present a totally constructive procedure that is most up to date after many works of Hironaka, H. (Ann. of Math,1964, and J.Hopkins U.,1977), Youssin, B. (Mem.AMS,1990), Aroca, JM, et al(Inst."J.Juan",1977), and Bierstone,E.,Milman,P.D.(Inv.Math.,1997), for instance.

1991 *Mathematics Subject Classification*. Primary(14E15); Secondary(14J17), (32S45).