

1. Prove that the following identities are valid in any Boolean algebra:

- (a)  $x \vee x = x$  (idempotent law)
- (b)  $x \vee 1 = 1$
- (c)  $(x \wedge y) \vee x = x$  (absorption law)
- (d) What are the duals of these identities?

2. Let  $x$  and  $y$  be elements of a Boolean algebra. Prove that  $x \vee y = y$  if and only if  $x \wedge y = x$ .