

Show all work for full credit, use correct notation, and clearly mark your answer.

1. For a fully continuous 5-year endowment insurance issued to  $(40)$ , you are given:
  - (i) The death benefit is 1000.
  - (ii) The pure endowment is 1000
  - (iii)  $\mu_x = 0.01$  and  $\delta_t = 0.04$
  - (iv) The annual gross premium rate at time  $t$  is  $\pi_t = 45$
  - (v) Non-settlement expenses are paid continuously at a rate of  $e_t = 10$
  - (vi) All reserve statements refer to gross premium reserve
    - (a) Determine the reserve at time 5.
    - (b) Use Thiele's differential equation to determine an expression for the derivative of the reserve at time  $t$ .
    - (c) Use Euler's Forward Equation with  $h = 0.5$  to determine an approximate value of  ${}_{4.5}V$
  
2. For a fully discrete whole life insurance on  $(x)$ , you are given:
  - (i) The death benefit is 10,000.
  - (ii) The withdrawal benefit for year 11, paid at EOY, is 1500.
  - (iii) The annual gross premium is 300.
  - (iv) Expenses paid at the beginning of year 11 are 3% of gross premium
  - (v)  $v = 0.9$ ,  $q_{x+10}^{(d)} = .02$ , and  $q_{x+10}^{(w)} = .10$
  - (vi) The asset share at time 11 is 230.

Determine the asset share at time 10.

3. For a fully discrete whole life insurance of 1000 on  $(x)$ , you are given:

- (i) Death is the only decrement
- (ii) The annual gross premium is 100
- (iii) First year expenses are 60% of gross premium, payable at BOY
- (iv)  $i = .10$
- (v)  $q_x = .03$
- (vi) Reserves at time 0 and time 1 are both equal to 0.

Determine

- (a)  $Pr_1$

Now suppose the values for interest, expenses, and mortality above are expected values, and that the actual values for interest and mortality are  $i = 0.08$  and  $q_x = .02$ , respectively, and the actual expenses were equal to the expected expenses.

Determine

- (b) the total gain per policy for year 1
- (c) the gain from interest prior to the calculation of any other gains by source
- (d) the gain from mortality after the gain by interest has been calculated, but prior to the calculation of the gain by expenses.

4. Suppose for a given 3-year product issued to  $(x)$ , you are given:
- (i) the annual premium is 50, payable at the beginning of each year
  - (ii) the profit vector is  $Pr = (-300, 260, 60, 20)$
  - (iii)  $p_x = 0.95$  and  $p_{x+1} = 0.92$
  - (iv) Profits are discounted using  $i = 0.05$

Determine

- (a) the discounted payback period
  - (b) the profit margin
  - (c) show that the internal rate of return is between 8% and 10% by showing that the net present value when calculated at 8% is positive whereas the net present value when calculated at 10% is negative.
5. For a universal life policy with a face amount of 50,000, you are given:

(i)

Policy Year	Annual Premium	Percent of Premium Charge	Annual Expense Charge	Annual COI rate Per 1000	Interest Credited
2	3000	7%	10	3	5%

- (ii) The account value at the end of year 2 is 5500.
- (a) Determine the account value at the end of year 1 if the policy is Type A.
- (b) Determine the account value at the end of year 1 if the policy is Type B.

6. Kathy entered a defined benefit plan on 1/1/1990 at age 35 with a salary in 1990 of 50,000. You are given:

- (i) The annual retirement benefit is 2% of the final 3-year average salary for each year of service, payable annually beginning at age 65.
- (ii) Kathy receives salary increases of 3% every January 1.
- (iii) Death is the only pre-retirement decrement.
- (iv) Mortality follows the Illustrative Life Table and  $i = 0.06$ .

Determine, as of the 1/1/2000 valuation date,

- (a) the actuarial liability of Kathy's retirement benefit using the traditional unit credit cost method
- (b) the normal cost of Kathy's retirement benefit using the traditional unit credit cost method
- (c) the actuarial liability of Kathy's retirement benefit using the projected unit credit cost method
- (d) the normal cost of Kathy's retirement benefit using the projected unit credit cost method