

Each problem is worth 10 points. Show all work for full credit, and use correct notation.

1. For a whole life insurance of 10,000 with semi-annual premiums on (80), you are given:

(i) Gross premiums of 600 are payable every 6 months starting at age 80

(ii) There is a percent of premium expense of 10%

(iii) The death benefit is paid at the end of the quarter of death

(iv) $i^{(4)} = 0.08$

(v)

| t | l_{90+t} |
|------|------------|
| 0 | 1000 |
| 0.25 | 900 |
| 0.50 | 810 |
| 0.75 | 720 |

(vi) ${}_{10.75}V = 750$

Calculate ${}_{10.25}V$.

2. Andy and Cathy are two 30-year olds. They each purchase a 35-year deferred whole life annuity due with annual payments of 10,000 by paying level annual net premiums at the beginning of each year during the deferral period.

Cathy's annuity contains a return of premium feature whereby during the deferral period, a death benefit equal to the return of premiums with interest is paid at the end of the year of death. Andy's annuity contains no such feature.

Using SULT actuarial assumptions, determine the value of $C - A$, where C denotes Cathy's premium and A denotes Andy's premium.

3. For a fully continuous 5-year endowment insurance issued to (40), you are given:

- (i) The death benefit at time t is $S(t) = 100t$
- (ii) The pure endowment is 500
- (iii) $\mu_{x+t} = 0.001 \cdot (1.1)^{x+t}$ and $\delta_t = 0.01t$
- (iv) The annual gross premium rate at time t is $\pi_t = 2 + t$
- (v) Non-settlement expenses are paid continuously at a rate of $e_t = 1 + 0.5t$
- (vi) The settlement expense, paid upon death at time t , is $10t$
- (vii) There is no settlement expense for the pure endowment
- (viii) All reserve statements refer to gross premium reserve

Use Euler's Backward Equation with step size 0.5 to approximate ${}_4V$.

4. A life insurance company issues 5000 fully discrete whole life insurance policies of 10,000 to independent lives age 50. You are given:

- (i) The annual gross premium is 250 per policy
- (ii) At the end of the third policy year, there are 4800 policies in force
- (iii) During the fourth policy year:

There was a per policy expense of 25 paid at the BOY
There were 50 deaths.
The earned interest rate was 6%.

- (iv) The reserve values are ${}_3V = 500$ and ${}_4V = 670$

Calculate the total profit for the fourth policy year for all policies in force at the beginning of the year.

5. A life insurance company sells a portfolio of 1000 fully discrete whole life insurance policies of 500, on lives age 45. You are given:
- (i) There are no expenses.
 - (ii) The annual gross premium is 9 per policy
 - (iii) At the end of the third policy year, there are 980 policies in force, and the reserve per policy is 20.
 - (iv) During the fourth policy year, there were 10 deaths, and at the end of the fourth policy year, the reserve per policy is 30.

Determine the interest rate earned during the fourth policy year, assuming there was no gain or loss during the year.

6. A life insurance company issues fully discrete 20-year term insurance policies of 1000 to 10,000 independent 45 year olds. You are given:
- (i) Expected mortality follows the SULT.
 - (ii) During the first two years, there were a total of 10 actual deaths.
 - (iii) During the third year, there were 6 deaths.
 - (iv) The gross reserve per policy at the end of year 3 is ${}_3V = 4$

Calculate the company's total gain due to mortality for the third year, for all policies in force at the beginning of the third year.

7. For a fully discrete 3-year term insurance policy issued to (55), you are given:
- (i) $q_{55+k} = 0.01 + 0.005k$, for $k = 0,1$
 - (ii) Pre-contract expenses are 100.
 - (iii) $Pr_1 = -16$ $Pr_2 = -12$ $Pr_3 = 168$
 - (iv) The hurdle rate is 10%.

Calculate the net present value of this policy.

8. For a fully discrete 2-year term life insurance on (50), you are given:

- (i) The annual gross premium is 250.
- (ii) The hurdle rate is 10%.
- (iii) The profit vector is $\overrightarrow{Pr} = \langle -165, 100, 125 \rangle$.
- (iv) The profit margin for this insurance is 6%.

Calculate the probability that (50) will survive one year.

9. For a 5-year insurance policy on (65), you are given:

- (i) The profit signature is $\overrightarrow{\Pi} = \langle -450, 250, 175, 75, 100, 150 \rangle$
- (ii) The risk discount rate is 10%.

Calculate the discounted payback period for this policy.

10. For a 3-year term insurance on (x), you are given:

- (i) the profit vector is $\overrightarrow{Pr} = \langle -500, 375, 100, 100 \rangle$
- (ii) mortality follows a constant force model
- (iii) the internal rate of return for this product is 6%

Determine q_x .