MAP 4176 / 5178 Test 7

Name:\_\_\_\_

Date: February 27, 2018

Each problem is worth 10 points. Show all work for full credit, and use correct notation.

1. Given  $q_{75} = .02$  and d = 10% determine the standard deviation of the present value random variable for a 2-year temporary annuity due issued to (75) with the first year's payment equal to 1500 and the second year's payment equal to 2000.

- 2. For independent lives (x) and (y), you are given:
  - (i) Mortality for (*x*) follows a constant force model with  $\mu_x = 0.02$
  - (ii) Mortality for (*y*) follows a constant force model with  $\mu_v = 0.04$

You are also given  $\delta = 0.03$ .

Determine the variance of the present value random variable for a continuous annuity that pays an annual rate of 9 per year until the earlier of the death of (*x*) and (*y*). (Recall that for independent lives,  $\mu_{xy} = \mu_x + \mu_y$ )

3. Use SULT actuarial assumptions and the claims acceleration approach to calculate the variance of the present value random variable for a whole life annuity due issued to (20) with quarterly payments of 250. Note that  $i = 0.05 \Rightarrow d^{(4)} = 0.04849$ .

4. Use SULT actuarial assumptions and assume a uniform distribution of deaths between integer ages to determine the variance of the present value random variable for a continuous 10-year temporary annuity of 100 per year issued to (20).

5. For a given annual effective interest rate *i*, you are given:

(i) 
$$A_x^{(12)} = 0.7$$

(ii)  $\ddot{a}_x^{(12)} = 10$ 

Determine *i*.